

Lab 4: Atmospheric Humidity Model Answers

Check your answers by:

- 1) Reviewing the interpretive answers to see how they make sense /match the model answer wording. Your answers should also make sense when considering the information shown by the two UNBC Wx Station graphs (at the end of this key). The last UNBC graph shows the weather that occurred during your lab.
- 2) Reviewing your calculation process /method and checking that your answer's units match those in the model answers.

Remember: For all model answers report and use your measurements in your assignment. Do not alter your assignment values to match those in the model answer key. If you have errors, fix them by using the correct methods or values (i.e. to calculate the mixing ration (r) you must use station pressure not sea level pressure, etc.).

See your Lab instructor if you can't determine whether your answers are correct before second submission.

Required information is highlighted yellow.

Lab 4 Model Answers:

1. **Humidity Lab Table 1:** Group #: **XX** Recorder: **XX (first & last name)**

Date of measurements: **(your Lab date) Feb XX /20XX** Partner(s): **XX (list all, first & last names)**

Station pressure (hPa) at the time of measurements (from roof data): **922.2 hPa** ←get values from your TA if needed

This is the station pressure from the UNBC Weather Station website at the time of your data collection. Unless you are in a pressurized building both the inside and outside air pressure measurements are the same.

Ambient weather conditions: 100% overcast; just below freezing, no precipitation

[report the outside weather conditions during data collection]

Observations:	Sling Psychrometer	Home-use Hygrometer	Assman type Psychrometer	Roof Data (Vaisalla probe)	
Inside: Location 1 = classroom 8-129 (Teaching Lab)					
Location 1 time: 13:30	T (°C)	21.5 °C	20 °C	22.4 °C	N/A
	T _w (°C)	15.0 °C	N/A	14.8 °C	N/A
	RH (%)	50% (Table interpolation)* [50.0% -- calculated from $e = 12.7$ hPa]	56 % (hygrometer reading)	43% (Table interpolation)* [44.5% -- calculated from $e = 11.8$ hPa]	N/A
Inside: Location 2 = Bentley Centre Hallway /					
Location 2 time: 13:56	T (°C)	20.0 °C	N/A	19.8 °C	N/A
	T _w (°C)	13.0 °C	N/A	11.8 °C	N/A
	RH (%)	44.2% (calculated from $e = 10.38$ hPa) [42.5% -- Table interpolation]	N/A	36.8% (calculated from $e = 8.47$ hPa) [37% -- Table interpolation]	N/A
Outside: Teaching Lab Roof (Building 8)					
Outside time: 13:42	T (°C)	-10.5 °C	-10 °C	-10.8 °C	-10.45 °C (roof 3 m temp)
	T _w (°C)	-11 °C	N/A	-11.2 °C	N/A
	RH (%)	76.5% (Table interpolation)* [80% -- calculated from $e = 2.009$ hPa]	90 % (hygrometer reading)	78% (Table interpolation)* [84% -- calculated from $e = 2.1172$ hPa]	74.1 %

* Though you are asked to use Tables 4.1 and 4.2 to determine Relative Humidity (RH) in Table 1 above, this isn't always possible for some humidity conditions (table values don't span the wide range of temperatures we can experience). If this occurs during your lab, calculate the values instead. For comparison, both Table 4.1 /4.2 and calculated values are reported above..

2. **Humidity Calculations:** For atmospheric pressures use hectopascals (hPa) as the standard unit

- Units must be properly tracked.
- RH must be calculated.
- Interim results must contain sufficient significant digits to not limit future calculations.

a) *Your answers depend on your measured values. Check your answers by confirming your units and methods are correct; your process should be the same as the model calculations below. See your Lab instructor if you aren't sure that your answers are correct.*

Table 2: Humidity Measure		INSIDE- classroom (Taylor Sling Psychrometer # 3)	OUTSIDE (Taylor Sling Psychrometer # 3)
	T	21.5 °C	-10.5 °C
	T_w	15.0 °C	-11 °C
i)	e	12.71 hPa (or 1271 Pa)	11.14 hPa (or 1114 Pa)
ii)	r	8.69 g kg ⁻¹	7.61 g kg ⁻¹
iii)	vpd	12.79 hPa (or 1279 Pa)	1.56 hPa (or 156 Pa)
iv)	RH	49.8%	87.7%
v)	T_d	10.5 °C	8.5 °C
vi)	ρ_v	$9.34 \times 10^{-3} \text{ kg m}^{-3}$	$8.50 \times 10^{-3} \text{ kg m}^{-3}$

For your sample calculations: Always identify the values used in each calculation at the start of the example calculation answer. The labels i) to vi) in Table 2 above match the following example calculations below.

Note: The notation $e^*_{(T_w)}$ indicates \rightarrow read the saturation vapour pressure curve (e^* vs T graph) at the wetbulb temperature (T_w) \rightarrow NOT e^* is multiplied by T_w .

These sample calculations use the INSIDE T and T_w measurements listed in Table 2 above.

i)

$$T = 21.5^{\circ}C \quad T_w = 15.0^{\circ}C \quad \lambda = 66 \frac{Pa}{^{\circ}C} = 66 \frac{Pa}{^{\circ}C} \times \frac{1hPa}{100Pa} = 0.66 \frac{hPa}{^{\circ}C}$$

$$e = e^*_{(T_w)} - \lambda (T - T_w)$$

$$e = 1700Pa - 0.66 \frac{hPa}{^{\circ}C} (21.5^{\circ}C - 15.0^{\circ}C)$$

$$e = 12.71hPa$$

ii)
$$r = \frac{0.622 \times e}{P - e} \times 1000 \frac{\text{g}}{\text{kg}} \quad P = \text{Stn. Pressure} = 922.2 \text{ hPa} \quad e = 12.71 \text{ hPa}$$

$$r = \frac{0.622 \times 12.71 \text{ hPa}}{(922.20 - 12.71) \text{ hPa}} \times 1000 \frac{\text{g}}{\text{kg}}$$

$$r = 8.69 \frac{\text{g}}{\text{kg}}$$

iii)

$$e_{(T)}^* = 25.50 \text{ hPa} \quad e = 12.71 \text{ hPa}$$

$$vpd = (e_{(T)}^* - e) = (25.50 - 12.71) \text{ hPa} = 12.79 \text{ hPa}$$

iv)

$$e_{(T)}^* = 25.50 \text{ hPa} \quad e = 12.71 \text{ hPa}$$

$$RH = \frac{e}{e_{(T)}^*} \times 100\% = \frac{12.71 \text{ hPa}}{25.50 \text{ hPa}} \times 100\% = 49.8\%$$

iv)

$$T_d = 10.5^\circ\text{C}$$

This is found using the e vs T_d graph and locating e on the hPa side of the of the graph and reading the corresponding dew point temperature (T_d) from the temperature axis. [Understand that the saturation vapour pressure – temperature curve, is also the vapour pressure - dew point curve.]

vi)

$$e = 12.71 \text{ hPa} \quad R_v = 4.62 \frac{\text{hPa m}^3}{\text{kg K}} \quad T = 21.5^\circ\text{C}$$

$$e = \rho_v R_v T \quad \text{rearrange to: } \rho_v = \frac{e}{R_v T} \quad \text{Note: } ^\circ\text{C} + 273.15 = \text{K}$$

$$\rho_v = \frac{12.71 \text{ hPa}}{\left(4.62 \frac{\text{hPa m}^3}{\text{kg K}}\right) (21.5^\circ + 273.15) \text{K}} = 9.34 \times 10^{-3} \frac{\text{kg}}{\text{m}^3}$$

- b) Identify sources of error (human, method, and instrument) associated with using each of the instruments in this lab. Comment on which instrument you think is most precise, least precise, and why.

Instruments Used:

- Home Hygrometer (a mechanical spring temperature & humidity sensor)
- Sling psychrometer and Assmann psychrometer – both use psychrometry to measure humidity
- [Vaisälä Temperature RH probe (don't consider its error as we don't provide such information in this lab)]

Home-use (mechanical) hygrometer: because of its design (bi-metallic strip technology) measurements are coarse with between +/-5% up to +/-15% uncertainty. Units of the same type have high variability. The instrument's materials and precision are not indicated on inexpensive models, and can change without notice. It is most likely to have large calibration errors, and is not reliably adjustable. Unfortunately reading errors are often not fixed even after the instruments are re-calibrated. Mechanical hygrometers work best in the 30% to 90% RH range. They are most often used for tracking large humidity changes over long periods of time. Most are used in homes, especially basements to understand if mold growth could be a problem. Mechanical hygrometers respond to humidity changes very slowly.

▪ **Human error:**

- Reading the scale improperly
- reading before the instrument has adjusted to its surroundings
- poorly situating the instrument

▪ **Method errors:**

- Large calibration errors and considerable hysteresis
- is not adjustable so readings can't be corrected even if calibrated
- no dry end calibration

▪ **Instrument error:**

- bi-metallic strip technology has a measurement uncertainty between +/-5% up to +/-15% (or more)
- coarse precision of the instrument scale
- works best in the 20% to 90% RH range

Both sling and Assmann psychrometers use psychrometry to determine humidity. Psychrometry is the standard method for directly measuring humidity. It is used as the calibration standard for other humidity sensors. Instrument accuracy depends on the quality of the thermometers used, the ability to aspirate the thermometers properly, and ensuring the wet bulb thermometer is moist (or properly frozen if below zero temperatures) while measurements are being made.

Sources of error for the sling psychrometer and the Assman psychrometer readings include (*always rank your error lists from largest to smallest impacts*):

▪ **Human errors:**

- mistakes in reading high precision temperatures scales accurately (Assmann psychrometers most affected)
- not wetting the wet bulb thermometer properly or accidentally wetting both thermometers; not using deionized water or having dirty wet bulb socks (as this alters evaporation rates)
- leaving insufficient time for the wet bulb temperature to reach an equilibrium value before taking a measurement
- insufficient ventilation of the wet bulb (Sling psychrometers most affected. This is less of a problem with the Assman psychrometers as its ventilation rate is regulated).

▪ **Method error:** Few issues (if there are any they are associated with ventilation and wet-bulb wetting; since these can be controlled if the equipment is properly cared for, they are really human errors)

▪ **Instrument error:** Thermometer quality determines how precisely each thermometer can sense the temperature; this depends on the thermometer bore trueness /quality which makes more accurate readings, and the diameter of the bore with thinner bores being able to measure with greater precision. The greater the thermometer cost, the greater the precision.

Most Precise/Least Precise and Why:

Of our instruments, the most accurate and precise are the Assman type psychrometers; they have:

- the most precise thermometers – they can be read to 0.1 of a degree
- the most accurate thermometers – their thermometers are manufactured with thin, high quality even bores (i.e. they few if any irregularities along the tube lengths)
- the most responsive thermometers – as they have very thin bores

- a regulated ventilation rate for the wet bulb – either motorized or wind-up motor
- thermometers that are shielded from radiation if situated poorly they are less affected

c) Which of the above measures of humidity (e , r , vpd , RH , T_d , ρ_v) are of use in comparing the actual amounts of moisture in the outside and inside air? [HINT: think about which measures of humidity depend only upon the amount of water vapour, and not upon other quantities.]

Only e , r and T_d are useful when comparing the actual moisture content of inside and outside air.

This is because the other measures of humidity (vpd , RH , ρ_v) depend on differences in temperature as well as differences in moisture content. Consequently, it is impossible to separate a variation in humidity caused by temperature from a variation in humidity caused by moisture. For example, relative humidity indicates how close air is to saturation and is used frequently as it is a comfort index. It can change in response to moisture or air temperature changes. (see Lab 4 slides regarding RH issues).

Because e and T_d are directly related to each other through the saturation vapour pressure curve (i. e. the e vs T_d graph), they only depend on the amount of moisture in the air and the atmospheric pressure (i.e. total air pressure). Since air pressure inside and outside is the same (unless you are in a pressurized building), e and T_d are suitable for comparing inside and outside humidity.

[Note: with rising or falling atmospheric pressure (i.e. air pressure changes due to changes in altitude or weather systems), e and T_d will vary due to changes in pressure. However, when indoor and outdoor humidity measurements are made under the same air pressure, e and T_d do show moisture content differences.]

The only humidity measure that depends solely on moisture content is r . Consequently, it is suitable for comparing inside and outside humidities, and moisture content at different altitudes in the atmosphere.

d) Explain any humidity differences between the locations.

Comparing your inside and outside e values will indicate if there are real moisture differences. The key in explaining your answer is to think about moisture sources and sinks in the two different environments.

In these model answers the inside classroom moisture was a bit higher than the outside moisture (even though the outside RH is almost double the inside RH). The capacity of cold air to hold moisture is smaller, consequently the outside RH is higher even though the moisture is less. The actual moisture content (e) inside is greater than that outside because wet shoes, clothes, and perspiring / breathing humans are moisture sources. In some buildings humidifiers can add moisture to inside air to make the RH more comfortable. UNBC doesn't currently use humidifiers. What does your data show?

e) If the heating system indoors jammed, and temperatures rose considerably what would happen to the values of e , RH , T_d , r ?

Moisture values that do not depend on temperature will not change. So, e , T_d , and r will not change. Because RH depends on temperature, it will decrease when the temperature goes up.

3. A cool winter Canadian air mass with a temperature of -4°C and a relative humidity of 91% meets a warm air mass sweeping northward from Texas with a temperature of 17°C and a relative humidity of 28%. In the mixing process will the southern border of the Canadian air gain or lose water vapour content? Calculate and explain.

This question requires you to work out actual moisture content of the two air masses and then compare them. The given RH values cannot be used directly for comparison because the temperatures of the two air masses are not equal. The airmass with the highest actual moisture content will lose moisture when it mixes with the drier airmass.

Determine the moisture content (e) for the Canadian air mass:

$$T = -4^{\circ}\text{C}$$

So from figure 4.1: $e^*_{(-4)} = 4.40 \text{ hPa}$ and using:

$$RH = \frac{e}{e^*_{(T)}} \times 100\% \quad \text{rearrange to: } e = e^*_{(T)} \times \frac{RH}{100\%}$$

$$e_{\text{Canadian air mass}} = 4.40 \text{ hPa} (0.91) = 4.004 \text{ hPa} = 4.00 \text{ hPa}$$

Then determine the moisture content for the Texas air mass:

$$T = 17^{\circ}\text{C} \quad \text{therefore:}$$

$$e^*_{(17)} = 19.50 \text{ hPa}$$

$$RH = \frac{e}{e^*_{(T)}} \times 100\% \quad \text{rearrange to: } e = e^*_{(T)} \times \frac{RH}{100\%}$$

$$e_{\text{Texas air mass}} = 19.5 \text{ hPa} (0.28) = 5.46 \text{ hPa}$$

By determining e for both air masses we know that the Texan air is actually more humid (i.e. have more moisture content). In mixing with the Texan air mass, the southern border of the Canadian air will become more humid and increase its moisture content.

See over for more about the conditions the day you made observations.

2024 UNBC Wx Stn GRAPH for our observation days

Below is the UNBC Wx Station graph for our week of humidity observations (each short tick mark = 3 hours).

In 2024 Tue labs had clearer skies than Wed labs (seen by the lower Tue $L\downarrow$ values). On Tues, when there were clouds, they were thin and few to scattered, creating spiky $K\downarrow$ values. On Wed, the more uniform cloud was thicker, reducing the radiation to about half of the Tue values. The pressure was rising on Tue after a high windstorm on Monday night; then falling on Wed.

Notice how air temperature (T - red plotted line) and the relative humidity (RH - fluorescent blue line) mirror each other for the 2 days of labs; this shows how RH is dependent on temperature.

While the dew point temperature (Td - dark blue line) shows how actual water vapour in the air changed over the 2 days of labs. Td dropped as the pressure increased and skies were clearer and then rose again on Wed when the conditions were cloudier.

2024 GRAPH Lab times: Tues Jan 30 (AM & midday) & Wed Jan 31 (AM & midday)

UNBC Lab roof-top weather station (10 min avg) on Wed Jan 31 20:13:02 PST 2024

